



CIAO

Collective Intelligence Algorithm for Optimisation

A tool for numeric optimisation of bound-constraint cost functions using collective intelligence simulation

User Guide

Version 1.24

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Bogotá, Colombia, May 2024

CIAO Version 1.25 - User guide

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*First Edition, May 2024
Bogotá, Colombia*

Overview

CIAO stands for *Collective Intelligence Algorithm for Optimisation*, and is a tool designed to find approximate solutions to optimisation problems whose decision variables take numeric values in the real domain, inspired in the mechanisms of the collective intelligence genome. The software is designed for an academic audience interested in the field of metaheuristics, as an user-friendly visual tool to conduct simulation experiments with a set of benchmark optimisation problems.

The approach of solving an optimisation problem with a collective of artificial agents undergoing an adaptation process is known as a population-based metaheuristics. Instead of using mathematical analysis of aggregated variables describing the phenomena, this approach resorts to modelling the interaction of a group of agents in a simulated environment and trace the evolution of such variables as they interact during the simulation process. In this way, **CIAO** enables the visual inspection of the emerging patterns of agents' self-organisation, in response to changes in the simulation parameters, which can provide useful insights regarding the adaptability of the algorithm to the hidden properties of the problem.

CIAO v1.25 has been released under GNU General Public License (GPLv3); it is available online at:

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Chapter 1

Description of the tool

1.1 What is CIAO?

The **CIAO** (Collective Intelligence Algorithm for Optimisation) metaheuristic simulates a collective intelligence approach to solving unconstrained continuous optimisation problems. It involves agents known as solvers (wolves) and users (dogs), navigating a solution space to find the optimal coordinates that minimise a cost function associated with an optimisation problem. This tool implements the algorithm as an agent-based model using the Netlogo language.

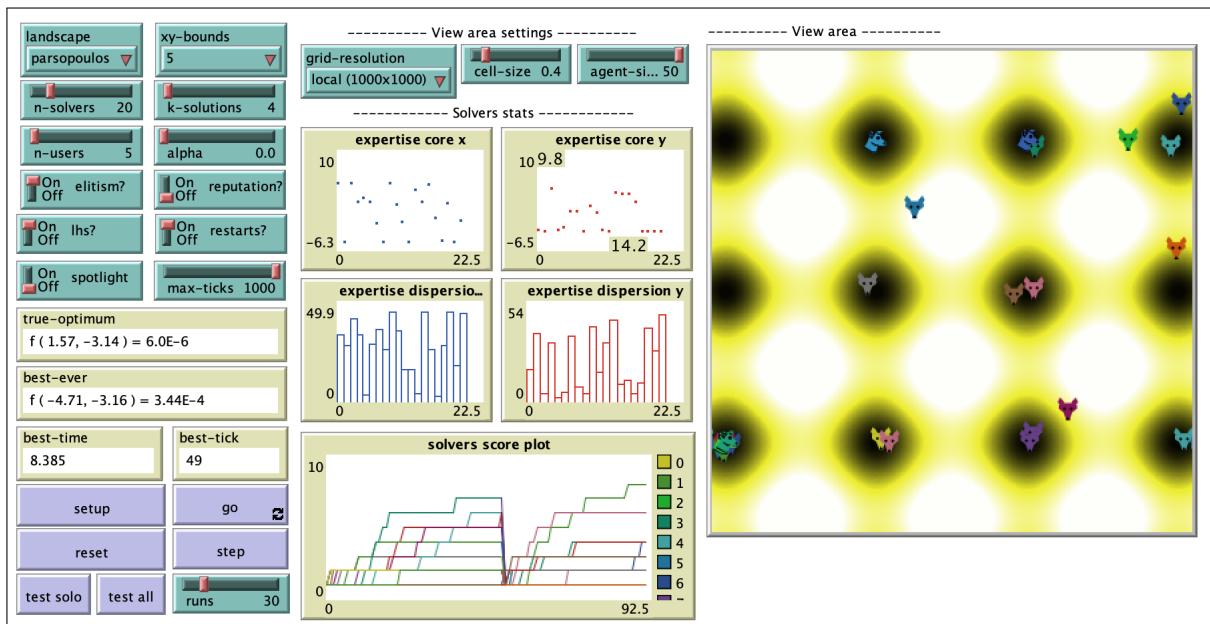
1.2 How it works

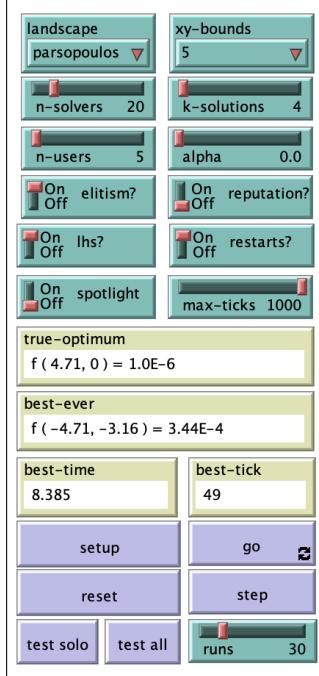
Solver agents maintain knowledge about promising sub-regions in the search space, represented as Gaussian distributions, involving their core expertise and their expertise dispersion. Users seek solutions from solvers, and the model incorporates learning and reputation mechanisms to refine the solver's expertise and reward effective solutions.

1.3 How to use it

Firstly, configure the simulation parameters in the simulation user interface:

- **LANDSCAPE:** Chooses the optimisation problem, visually represented in the view or world area. Selection influences the XY-BOUNDS. Refer to the APPENDIX: LIST OF BENCHMARK PROBLEMS section for a description of available benchmark functions.
- **XY-BOUNDS:** Sets the lower and upper bounds of the search space depending on the chosen landscape.
- **N-SOLVERS:** Defines the number of solver agents.





- **K-SOLUTIONS:** Defines the number of solutions a chosen solver attempts to generate.
- **N-USERS:** Defines the number of user agents.
- **ALPHA:** Sets the learning rate for solver adaptation.
- **ELITISM?**: Activates the elitism mechanism, which ensures that the best solution found in the current generation is passed on as the center of expertise for one of the solvers in the next generation of the algorithm.
- **REPUTATION?:**: Enables or disables choosing solvers based on their scores using roulette wheel selection.
- **LHS?:**: Enables or disables Latin Hypercube Sampling of the initial solver population.
- **RESTARTS?:**: Enables or disables random resets to prevent stagnation due to premature convergence to local minima.
- **SPOTLIGHT?:**: Enables or disables highlighting the global minima in the view or world area.
- **MAX-TICKS:**: Sets the maximum number of iterations of the algorithm main search routine.
- **GRID-SIZE:**: Adjusts the resolution of the view area. Choose “*web (200x200)*” if running on the model online in the modelling commons website, as server memory constraints limit the amount of cells in the search space. Choose “*local (1000x1000)*” for a higher resolution of 1000x1000 cells if running on a desktop machine, allowing for better discretisation of the search space.

- **CELL-SIZE:** Specifies the size of each grid cell in the view area. Can be adjusted from 0.1 to 2 with a step increment of 0.1. This control enables closer or further inspection of the cells in the view area.
- **AGENT-SIZE:** Controls the size of agent representations in the view area. Adjusts from 10 to 50 with a step increment of 10.

A typical configuration of values for these parameters would be:

- N-SOLVERS: 10
- K-SOLUTIONS: 4
- N-USERS: 5
- ALPHA: 0.5
- ELITISM?: On
- REPUTATION?: On
- LHS?: On
- RESTARTS?: On
- MAX-TICKS: 1000

Next click the **SETUP** button to initialise the model with chosen parameters. And then click the **GO** button to start the simulation. Observe the movement and interaction of solvers and users in the view area of the simulator. You can control the execution of the simulation using the control panel buttons:

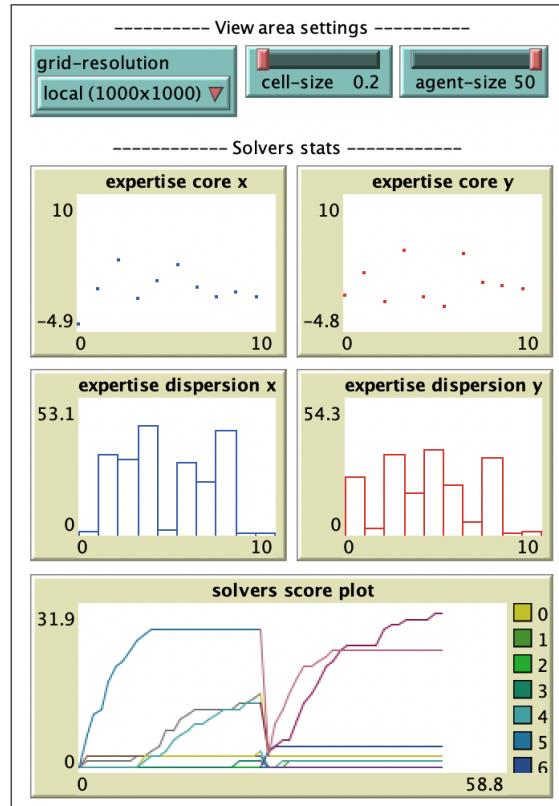
- **SETUP:** Computes and visualises the landscape and initialises agents and global variables of the simulation, according to the given parameters.
- **RESET:** Only initialises agents and global variables of the simulation, according to the given parameters. Also clears plots from previous runs.
- **GO:** Executes the main search routine until stopping conditions are met.
- **STEP:** Executes one iteration of the main search routine.

The model also features two buttons for test experimentation:

- **TEST SOLO:** Executes an experiment with the specified number of repetitions (i.e. RUNS), using the current configuration of model parameters for the selected LANDSCAPE. Results of each run are recorded as either a *hit* or a *miss* depending on whether the algorithm finds the optimum or not. The BEST-TICK, which indicates the time step at which the solution was found in each run, along with the overall success rate within the specified MAX-TICKS, is displayed in the COMMAND-CENTER panel.
- **TEST ALL:** Performs the same experiment but tests the specified number of RUNS on all benchmarks available in the LANDSCAPE list. Aggregated results showing the success rate for each experiment are displayed in the COMMAND-CENTER panel.

1.4 Other distinctive features

- Observe how solvers adapt their expertise to the search space, guiding users towards promising regions.
- Observe how regions with low (black) and high (yellow) values in the landscape are visualised in the view area based on the selected problem (LANDSCAPE).
- Watch the TRUE-OPTIMUM value and notice how the BEST-EVER approaches to it.
- Monitor the BEST-EVER patch, BEST-TICK, and BEST-TIME to understand when and where the best solution is discovered.
- Observe how the EXPERTISE CORE and EXPERTISE DISPERSION parameters of solvers evolve over time in the corresponding plots.
- Analyse the SOLVERS SCORE plot to see how solvers' reputation change during the optimisation process.
- Notice the periodic changes in the SOLVERS SCORE plot when RESTARTS? is enabled.



1.5 Try it yourself

- Experiment with different numbers of SOLVERS and USERS to observe how the collective intelligence adapts to problem complexity.
- Observe how adjusting the learning rate (ALPHA) affects the adaptation of solver expertise. Higher values (closer to 1) make solvers more resistant to exploring new solutions and cling to their currently known best solution. Lower values make them more susceptible to learning from new information and exploring alternative solutions.
- Evaluate the impact of greedy (utilising the single best new solution) and non-greedy (leveraging the average performance of multiple new solutions) learning strategies on solver adaptation using the GREEDY? switch.
- Explore the effects on solvers scores and on user decisions, of enabling or disabling reputation-based solver selection (REPUTATION?).
- Test the impact of Latin Hypercube Sampling of initial solver locations (LHS?).
- Observe the behaviour when random restarts are enabled or disabled (RESTARTS?).
- Toggle the spotlight (SPOTLIGHT?) to visually track the global minimum in the landscape, and how user agents approach to it.

As a side note, we remark that the resolution level can induce quantisation errors during the cost function sampling, therefore the optimum patch coordinates of a given LANDSCAPE can differ depending on the GRID-SIZE. For example, the optimum of ROSENBROCK'S problem is different for 1000x1000 and 200x200 resolutions.

1.6 Extending the tool

Some possible paths for tool extensions are:

- Extend the list of landscape functions of optimisation problems.
- Implement additional user or solver behaviours to enhance the complexity of the collective intelligence dynamics. Techniques such as temporal memory, tabu lists, collaboration mechanisms, or more advanced expertise representation models like a mixture of Gaussians.
- Extend the model to incorporate alternative solver selection strategies to compare their impact on the optimisation process.
- Generalise the model to handle continuous optimisation problems in more than two dimensions ($d > 2$).
- Investigate the adaptation of the model for binary domain problems, exploring how the dynamics change in this context.

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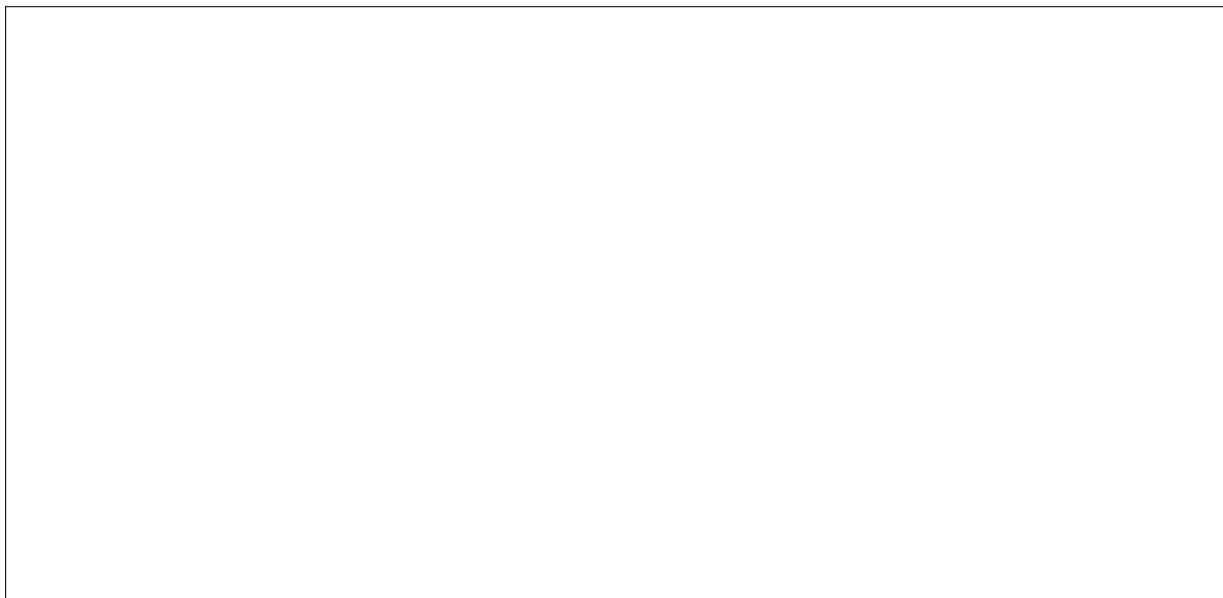
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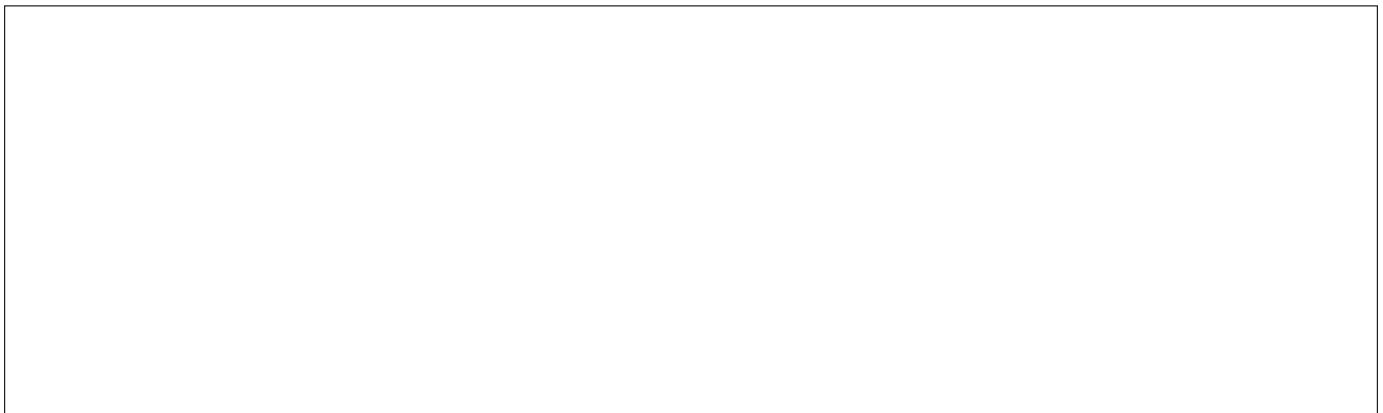
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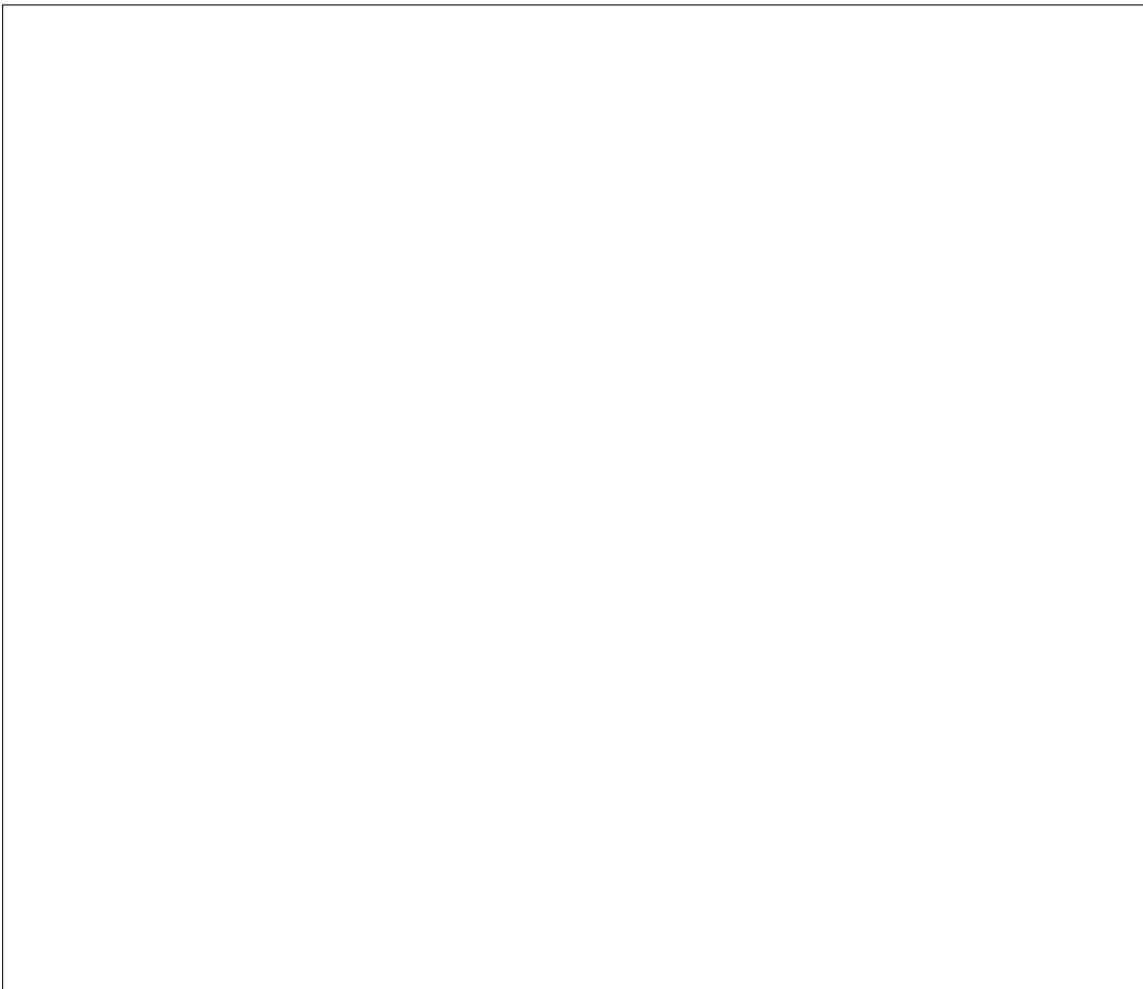
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)
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c _2 r ` / i ? 2 b Q H p Z` Q ` Q # i B M B M# 2 i i 2 ` b Q H m i B Q M
 i Q ` 2 r `/ @ b Q H p 2 ` (i ? 2 @ b Q H p 2 ` # 2 i i 2 ` @ T i + ?)
b F i ? 2 @ b Q H p 2 ` (
b 2 i b + Q ` 2 b + Q ` 2 Yc R M + ` 2 b 22 b Q H p ^ b ` 2 T m i i B Q M
K Q p 2 @ # 2 i i 2 ` @ T i + c ? J Q p 2 Q i ? 2 # 2 i i 2 ` b Q H m i B Q H M Q + i B Q M
b 2 i # t + Q ` c I T / i 2 i ? 2 b Q H p ^ b ` # 2 b i b Q H m i B b Q t M @ + Q Q ` / B M i 2
b 2 i # v + Q ` c I T / i 2 i ? 2 b Q H p ^ b ` # 2 b i b Q H m i B b Q V M @ + Q Q ` / B M i 2
)
 2 M /

c I T / i 2 i ? 2 b Q H p ^ b ` F M Q r H 2 / b 2 i ? 2 v b 2 ` + 7 Q ` M 2 r b Q H m i B Q M b
 i Q m T / i 2 @ b Q H p 2 ` (i ? 2 @ b Q H p 2 `)
b F i ? 2 @ b Q H p 2 ` (
H 2 i M 2 r @ t H 2 i M 2 r @ v c y A M B i B H P x 2 B # H Z l Q ` M 2 r + Q Q ` / B M i 2 b
b 2 i M 2 r @ t (t + Q `) K Q M @ Q M b 2 Q H M 7 i B Q M b (p H m 2)
b 2 i M 2 r @ v (v + Q `) K Q M b 2 Q H M 7 i B Q M b (p H m 2)
c I T / i 2 b Q H p ^ b ` + Q ` 22 t T 2 ` i B b # 2 b 2 / Q M i ? 2 H 2 ` M B M j 2
b 2 i K t U H T ? # t V Y U U R @ H T ? V M 2 r @ t V
b 2 i K v U H T ? # v V Y U U R @ H T ? V M 2 r @ v V
b 2 i t v K t K v c J Q p 2 ? 2 b Q H p 2 Q i ? 2 m T / i 2 H Q + i B Q M
c L `` Q r / Q r M ? 2 b Q H p ^ b ` 2 t T 2 ` i B b B b T 2 ` b B Q M
b 2 i b t b t 2 t T U @ X y y R U i B + F b K Q / 8 y V V
b 2 i b v b v 2 t T U @ X y y R U i B + F b K Q / 8 y V V
)
 2 M /

c * ? 2 + B 7 M v m b 2 ? b B K T ` Q p i 2 / 2 # 2 b i b Q H m i B 7 Q Q M n N / Q 7 `
 i Q m T / i 2 @ # 2 b i
H 2 i # 2 b i @ M Q b M @ Q M b 2 Q b (p H m 2)
B 7 (p H m 2) Q 7 # 2 b i @ M Q r I (p H m 2) Q 7 # 2 b i @ 2 p 2 ` (
 c _2 + Q ` i ? 2 H Q + i B Q i M + F - M / i B K 2 r ? 2 M M 2 r 2 # 2 b i @ 2 p b 2 Q H m i B r Q b M
 7 Q m M / X
b F # 2 b i @ M Q b 2 (# 2 b i @ 2 p T 2 i + ? @ ? 2) 2
b 2 i # 2 b i @ i B + F i B + F b
b 2 i # 2 b i @ i B K 2 i B K 2 `
)
 2 M /

c S 2 ` 7 Q i K 2 B M B i B b H i m T Q ` i ? 2 b B K m H i B Q M
 i Q b 2 i m T
+ H 2 ` @ H H c * H 2 ` i ? 2 r Q ` H / M / H H ; 2 M i b
b 2 i m T @ b 2 ` + ? @ H M / b o + a T 2 m T i ? 2 H M / b + T M / + Q b i 7 m M + i B Q M
b 2 i m T @ b Q H p 2 ` b c a 2 i m T b Q H p 2 ; 2 M i b
b 2 i m T @ m b 2 ` b c a 2 i m T m b 2 ` ; 2 M i b
b 2 i m T @ ; H Q # H b c a 2 i m T ; H Q # H ` B # H 2 b
)
 2 M /

c _2 b 2 i ? 2 b B K m H i B Q M M 2 r ` m M r B i ? Q m H i Q K T m i B M 2 ; H M / b + T ; 2 B M
 i Q ` 2 b 2 i
+ H 2 ` @ H H @ T H Q i b c * H 2 ` T H Q K Q M B i Q ` ` b Q K ? 2 T ` 2 p B Q ` m r b M
b 2 i m T @ b Q H p 2 ` b c _2 B M B i B H b Q h 2 p 2 ; 2 M i b
b 2 i m T @ m b 2 ` b c _2 B M B i B H n B b x 2 ; 2 M i b
b 2 i m T @ ; H Q # H b c _2 B M B i B H b Q 2 # H ` B # H 2 b
)
 2 M /

c a 2 i m T b Q H p 2 ; 2 M i b
 i Q b 2 i m T @ b Q H p 2 ` b

c * H 2 ` T ` 2 p B Q m Q H p 2 ; 2 M i b
b F b Q H p 2 ` b (/ B 2)

c * ` 2 i 2 b Q H p 2 ; 2 M i b
 + ` 2 i 2 @ b Q H p 2 ` b M @ b Q H p 2 ` b (
 c b b B ; M B b m H i ` B # m i 2 b
b 2 i b ? T 2 r Q H 2
b 2 i + Q H Q Y U R y r ? Q V
b 2 i b B x 2 ; 2 M i @ b B x 2

c A M B i B H B k T 2 ` i B b k 2 Q / 2 H M / b + Q ` 2
b 2 i K t ` M / Q K @ t + Q `
b 2 i K v ` M / Q K @ v + Q `
b 2 i b t ` M / Q K @ 7 H 8 Q i
b 2 i b v ` M / Q K @ 7 H 8 Q i
b 2 i # t K t
b 2 i # v K v
b 2 i b + Q` 2 R

c a 2 i B M B i B ` H M / Q H Q + i B Q M
b 2 i t v K t K v
)

c A 7 2 M # H 2 f ? M ; B Q + i B Q r l B b ? G i B M v T 2 ` + m # 2 K T H B W H ; ? W
**B 7 H ? b ** (H i B M @ ? v T 2 ` + m # 2 @ b K T H B M ;)
2 M /

c a 2 i m T m b 2 ` ; 2 M i b
i Q b 2 i m T @ m b 2 ` b
 c * H 2 ` T ` 2 p B Q m m b 2 ` ; 2 M i b
b F m b 2 ` b (/ B 2)

c * ` 2 i 2 M 2 r m b 2 ` b
 + ` 2 i 2 @ m b 2 ` b M @ m b 2 ` b (
 c b b B ; M B b m H i ` B # m i 2 b
b 2 i b ? T 2 / Q
b 2 i b B x 2 ; 2 M i @ b B x 2

c b b B ; M B i B Q H M # 2 b i b Q H m i B Q M
 K Q p 2 @ Q Q 2 @ T Q 7 + ? 2 b
b 2 i Q r M @ # 2 b i p H m 2
)

2 M /

c b b B ; M B i B p H H m 27 b Q ` ; H Q # H ` B # H 2 b
i Q b 2 i m T @ ; H Q # H b
b 2 i # 2 b i @ i B + F y
b 2 i # 2 b i @ i B K 2 y
b 2 i # 2 b i @ 2 p 2 ` K t @ Q M i 2 @ Q D p H m 2
` 2 b 2 i @ i B + F b
2 M /

c _ 2 b i ` i ; 2 M i b Q T ` 2 p 2 M b i i ; M i B Q M
i Q ` 2 b i ` i
 b 2 i m T @ m b 2 ` b
 b 2 i m T @ b Q H p 2 ` b
2 M /

c * ? Q Q b 2 b Q H p Z ` B i ? 2 ` M / Q K l Q v ; m B / 2 # v ` 2 T m i i B Q M
i Q @ ` 2 T Q` ? Q Q b 2 @ b Q H p 2 `
B 7 2 H W U` 2 T m i i B Q M \ V (
c * ? Q Q b 2 b Q H p Z ` b 2 / Q M i ? 2 B ` 2 T m i i B @ M B M ; ` Q m H 2 i i 2 2 2 H
H 2 i b + Q ` 2 @ H B b i K T ((i ? 2 @ b Q H p 2 `) @ = (b + Q ` 2) Q 7 i ? 2 @ b Q H p 2 `) b Q ` i b Q H
H 2 i B / @ H B b i K T ((i ? 2 @ b Q H p 2 `) @ = (r ? Q) Q 7 i ? 2 @ b Q H p 2 `) b Q ` i b Q H p 2 ` b

c * Q K T m+2n K m H i B p 2i` B # m i B Q Q M K ? 2 ? B b i Q ; ` Q K 7 b + Q ` 2 b
H 2i? B b i 7 T m i U H B b i U 7 B` b i b + Q ` 2 @ H B b i V V U # m i @ 7 B` b i b + Q ` 2 @ H B b i V
H 2i; ; b ` 2 / m + 2 ((+ m K m H M 2 t i) @ = b 2 M i 2 M + 2 + m K m H U U H b i + m K m H V Y M 2 t i

c l b 2 ` Q m H 2 i r 2 2 2 H Q + ? Q Q b 2 b Q H p 2 + Q ` / B M Q i ? 2 + m K m H i B p 2
 / B b i` B # m i B Q M
H 2iT Q + F 2 i b K T (T @ = T f H b i ; ; b c) Q K; b m i 2 2 2 H Q + F 2 # b
 M Q ` K H B x B n M K m H i B p 2 K
H 2i# H H M / Q K @ 7 H R Q i c _ Q H H P 2 # H H f ? 2 M f ? 2 + F ? 2
 r B M M Z` Q + F 2 i
H 2ir B M M 2` 7 B` b i 7 B H i 2` ((B M / 2 t) @ = # H H I 4 B i 2 K B M / 2 t T Q + F 2 i b) ` M ; 2
 H 2 M ; i ? T Q + F 2 i b
` 2 T Q` b Q H p 2` B i 2 K r B M M 2` B / @ H B b i
) (c P i ? 2` r B b + 2 Q Q b 2 v b Q H p 2 i ` M / Q K M B 7 Q ` K H v
` 2 T Q` Q M 2 @ b Q H p 2` b

)
2 M /

c S 2` 7 Q` K i B M v T 2` + m # 2 K T H B T M Q` B M B i B b H Q H p 2 f Q + i B Q M b
i Q H i B M @ ? v T 2` + m # 2 @ b K T H B M ;
c * Q K T m i 2 2 r B / i ? Q 7 H Q + i B Q M Q i b
H 2ir B / i ? k K t @ T t + Q M @ b Q H p 2` b

c a T H B 2 + ? / B K 2 M b B Q M M Q M @ Q p 2` H b T H Q b i D R T 2` b Q H p 2` M / b K T H 2
` M / Q K Q + i B Q r B b ? B M
7 Q ` 2 + ? ` M ; 2 k (B M / 2 t @ =
H 2i+ Q Q `/ B M i 2 b b ? m 7 7 H 2 M @ p H m 2 b M @ b Q H p 2` b (b H Q i @ = r B / i ? U b H Q i Y
` M / Q K @ 7 H R Q i)

c b b B ; M Q Q `/ B M H i Q + i B Q 7 M Q b 2 + ? ; 2 M i B M M Q `/ 2` H K M M 2 2 - M b m ` B M ;
Q m M / Q M b i` B M i b
U 7 Q ` 2 + ? b Q ` i b Q H p 2` b + Q Q `/ B M i 2 b (i ? 2 @ b Q H p 2` + Q Q `/ B M i 2) @ =
b F i ? 2 @ b Q H p 2` (B 7 2 H b 2 M / 2 t 4 y (c t @ + Q Q `/ B M i 2
b 2 i K t U @ t @ T t + Q ` + Q Q `/ B M i 2 V
b 2 i # t K t
b 2 i t + Q ` K t

) (c v @ + Q Q `/ B M i 2
b 2 i K v U @ t @ T v + Q ` + Q Q `/ B M i 2 V
b 2 i # v K v
b 2 i v + Q ` K v

))
) v

) V

2 M /

c _ 2 T Q` i 2 Q / B b T H b v Q H p 2` b + Q ` 2
i Q @ ` 2 T Q` i 2 Q r @ b + Q ` 2 b (i ? 2 @ ; 2 M i)
` 2 T Q` U r Q` i b r r ? Q] 4] b + Q ` 2 %] V

2 M /

c _ 2 T Q` i 2 Q / B b T H v 2 M b H Q + i B Q M
i Q @ ` 2 T Q` i 2 Q + i B Q M b (i ? 2 @ ; 2 M i)
` 2 T Q` U r Q` i m h r ? Q] , U T` 2 + B b B Q M] - t] R T` 2 + B b B Q M] W Q R

2 M /

c . 2 7 B M p 2 B 2 r ` 2 b 2 i i B M ; r b ? 2 M H Q / B M ? 2 K Q / 2 H
i Q b i` i m T
b 2 i ; ` B / @ ` 2 b Q H m j i B Q M k y t k y y]

c a i` i m T B i ? + 2 H H B x 2 R i Q T` 2 p 2 M b i B 2 r ` 2 / B b i Q` i B Q r M B M 2 b B x B M ;
UL 2 i G Q # Q m V
b 2 i + 2 H H @ b B x 2 R
b 2 i ; 2 M i @ b B x 2 R y

2 M /

V
)
 c a 2 i m T M ; 2Q 7p ` B # H 2 Q Q `/ B M 72Qb2 + ?T` Q # H 2 K
 b 2 i t v @ # Q m M B 2 H b 2 @ p H m 2
 H M / b + T 2 4 F H 2 v(j k)
 H M / b + T 2 #2 H 2 Q`
 H M / b + T 2 K 2 B + ? H 2 j B Q x
 H M / b + T 2 T 4 ` b Q T Q j H (8 b)
 H M / b + T 2 #4 Q ? + ? 2 b p M K J R (R y y)
 H M / b + T 2 #4 Q J ? Q`
 H M / b + T 2 +4 Q b b @ B M]@Q` v
 H M / b + T 2 / 4 t Q M @ T J` Q f 2
 H M / b + T 2 ?4 Q H / 2 ` @ i] # Q f 2
 H M / b + T 2 ?4 Q b F Q`
 H M / b + T 2 H 4 2 p v Q`
 H M / b + T 2 K 4 i v b Q`
 H M / b + T 2 K 2 B b ? ` M X j j Q`
 H M / b + T 2 K 4 B b ? ` M X j 8 Q`
 H M / b + T 2 K 4 B b ? ` M X j e Q`
 H M / b + T 2 p 4 B M + 4 M Q`
 H M / b + T 2 x 4 F ? ` Q R (R y)
 H M / b + T 2 / 4 K p M Y R (R 9)
 H M / b + T 2 2 4 ; ? Q H / 2 (8 R k)
 H M / b + T 2 ; 4 H / b i 2 B M @] T (B k +)
 c 6 Q ` i ? 2 7 Q H H Q r B M Q # H 2 K 2 - m b 2 ? 2 ` M ; 2 (@ j k - j k) B M b i 2 Q 7 i ? 2
 Q ` B ; B M (@ R y y R y -) i Q ` 2 / m + 2 B b + ` 2 i B x i B Q M Q ` b
 H M / b + T 2 2 4 b Q K Q`
 H M / b + T 2 b 4 ? 7 7 2 M X 9 Q`
 H M / b + T 2 b 4 ? 7 7 2 M X j k (j k)
 c 6 Q ` M v Q i ? 2 T ` Q # H 2 h b 2 (@ 8 - 8) / 2 7 m H i M ; 2
 (8)

V
 c 1 p H m i 2 2 + Q b i 7 m M + i B 7 Q M 2 + ? T i + ? B M i ? 2 H M / b + T 2
 b F T i + ? 2 b
 b 2 i t T t + Q` U t v @ # Q m M K bt @ T t + Q`
 b 2 i v T v + Q` U t v @ # Q m M K bt @ T v + Q`
 c L Q i 2 h ` B ; Q M Q K 2 7 n B M + i B Q 2 / l m B ` B M T n B i M / 2 ; ` 2 2 b M Q i / B M b i ? m b -
 + Q M p 2 ` b B Q f M Q U R 3 y T B r b m b 2 /
 b 2 i p H m 2
 b 2 H b 2 @ p H m 2
 H M / b + T 2 4 F H 2 v
 @ k y 2 t T U @ y B k i u y X 8 U t k Y v k v v v @ 2 t T Q U x R 3 y T B v
 U k T B t V Y Q U U R 3 y T B U k T B v V V V Y k y Y 2
)
 H M / b + T 2 #2 H 2 (U U R X 8 @ t Y U t v V V V k V Y U U k X k 8 @ t Y U t U v k V V V V k V Y U U k X e
 t Y U t U v j V V V k V)
)
 H M / b + T 2 #4 Q ? + ? 2 b p M K J R (U t k V Y k U v k V @ U y Q U U R B y T B j T B t V V V @ U y X 9
 + Q b U U R 3 y T B 9 T B v V V Y y X d)
)
 H M / b + T 2 #4 Q Q J ? (U t Y U k v V @ d V k Y U U k t V Y v @ 8 V k)
)
 H M / b + T 2 +4 Q b b @ B M]@ (i ` v
 @ y X y y y R # U U B U U R 3 y T B t V b B U U R 3 y T B v V 2 t T # U R y y
 @ U b U i U U t k V Y U v k V T V W V Y R V y X R V)
)
 H M / b + T 2 / 4 K p M Y E
 B 7 2 H b 2 @ p U H m 2 k V Q ` U v 4 k V (R y y)
 B 7 2 H b 2 @ p U H m 2 k V M / U v 4 k V (y)
 B 7 2 H b 2 @ p U H m 2 t @ k V I y X y y y R V # Q U v U @ k V I y X y y y R V (R y y)
 B 7 2 H b 2 @ p U H m 2 t @ k V I y X y y y R V # M / U v U @ k V I y X y y y R V (y)
 (U R @ # U U B U U R 3 y T B T B U t @ k V V V b B U U R 3 y T B T B U v
 @ k V V V V f T B U U k V U t @ k V U v @ k V V V V 8 V U U k Y U t @ d V
 k V Y U k U v @ d V k V V)

```

)
H M/b+ T2/3 t Q M @ T] E+2
  Ut @ RV k Y k UUk v kV @ tV k
)
H M/b+ T2/4 Q Tr ♂2
  @ R UUUR QUUR3yTfv Rk b[`iUUt kV Y Uv kVV VVV f UyX8
  UUt kV Y Uv kVV Y k VVV
)
H M/b+ T2/4 b Q K(
  @ R +Q b UUR3yTfv tV +Q b UUR3yTfv vVV 2tT U@b U@t @k
  Y Uv @b U U U V kVV
)
H M/b+ T2/4 ;? Q H J2( c MQi2? i /2;`22bMQi /B Mb-`2 M22/27Q` b B M m M+i B Q M
  U U@ tVb B MU UR3yTfv b[`i U #b Ut @ Uv Y 9dVVVVV @ Ub b YM 9dV
  U UR3yTfv b[`i U #b U Ut f kV Y Uv Y 9dVVVV
)
H M/b+ T2/4 ;? Q H/bi2 B M @JT( B+2
  UR Y UU t Y v Y RV kV URN @ UR9 tV Y Uj Ut kV @ UR9 vV Y Ue
  t vV Y Uj Uv kVV VVV
  Uj y Y UU UK tV @ Uj vV V kV UR3 @ Ujk tV Y URk Ut kV Y U9
  vV @ Uje t vV Y Ukd Uv kVV VVV
)
H M/b+ T2/4 ?B KK2 H#H m
  UU t KV Y v @ RR V k Y Ut Y Uv kV @ dV k
)
H M/b+ T2/4 Q H/2` @ i] #(H2
  @ R #Ub B MU UR3yTfv tV +Q b UUR3yTfv vV 2tT#U R @b [U iU t
  k Y v kV Tfv VVV
)
H M/b+ T2/4 Q b F B
  UR @ U3 tV Y Ud Ut kVV @ UU d f jV t jV Y UyXk8 Ut 9VV V
  UU v kV 2tT UU @ vVV V
)
H M/b+ T2/4 p]v(
  Ub B MU UR3yTfv TB UR Y Ut @ RV f 9VV kV
  Y UUUR Y Ut @ RV f 9V @ RV kV b B MU UR3yTfv U U B UR Y
  Ut @ RV f 9VV Y RV V kV
  Y UUUR Y Uv @ RV f 9V @ RV b B MU UR3yTfv U U k TB UR Y
  Uv @ RV f 9VV V kV
)
H M/b+ T2/4 K4 i v b(
  UyXke UU t KV Y Uv kVV V @ UyX93 Ut vVV V
)
H M/b+ T2/4 K4 B + ? H 2 jB(+x
  @ R b B MU UR3yTfv tV b B MU UR3yTfv R Ut kV TB VV U k
  R y V V
  @ b B MU UR3yTfv vV b B MU UR3yTfv k Uv kV TB VV U k
  R y V V
)
H M/b+ T2/4 K4 B b ? `M Xj(
  b[`i U #b U U R3yTfv b[`i U #b U Ut kV Y v VVV V Y y Xy R Ut Y vV
)
H M/b+ T2/4 K4 B b ? `M Xj8(
  UU b B MU UR3yTfv U Q b UUR3yTfv tV Y Q b UUR3yTfv vVV k VV
  k
  Y U Q b UUR3yTfv U B MU UR3yTfv tV Y b B MU UR3yTfv vVV k VV
  k Y tV kV
  Y U Xy R tV Y UXR vV
)
H M/b+ T2/4 K4 B b ? `M Xje(
  @ R HM b B MU UR3yTfv b Q b UUR3yTfv tV Y Q b UUR3yTfv vVV
  k VV k
  @ b Q b UUR3yTfv b B MU UR3yTfv tV Y b B MU UR3yTfv vVV k VV
  k Y tV kV
  Y X R UU t @ RV k Y Uv @ RV kV
)
H M/b+ T2/4 ` b Q T Q ♂( Q b
  + Q b UUR3yTfv tV k Y b B MU UR3yTfv vV k
)

```

k y

H M/b + T2`4bi`B; B M
 ky Y UU t kV @ RQUR3yTfV UK TB v VV t VV Y UU v kV @ Ry
)
 H M/b + T2`4bi`B; B Q#B TQ (
 ky Y UU Ut @ RXRkjV kV+@URy3yTfV UK TB Ut @ RXRkjVV
 Y UU v @ RXRkjV kV+@URy3yTfV UK TB Uv @ RXRkjVV
)
 H M/b + T2`4bi`B; B #B TQ (
 ky Y UU Ut Y RV kV @ QURy3yTfV UK TB Ut Y RVVV Y UU v
 @ RV kV @ RQUR3yTfV UK TB Uv @ RVVV
)
 H M/b + T2`4bi`B; B #B TQ (+F
 Ryy Uv @ Ut kV V k Y UR @ tV k
)
 H M/b + T2`4bi`B; B #B TQ (
 yX8 Y b#UR3yTfV Ut k @ v kV V kV @ yX8 f UR Y Uy Xyy R Ut
 k Y v kVV V kV
)
 H M/b + T2`4bi`B; B #B TQ (
 yX8 Y U#UR3yTfV b#UR3yTfV #Ut k @ v kV V V k @
 yX8 f UR Y Uy Xyy R Ut k Y v kVV V kV
)
 H M/b + T2`4bi`B; B #B TQ (
 t k Y v k
)
 H M/b + T2`4bi`B; B #B TQ (
 Ut @ jV k Y Uv Y jV k
)
 H M/b + T2`4bi`B; B #B TQ (
 Ut kV V @ URXy8 Ut 9VV Y UU t eV f eV Y Ut vV Y Uv kV
)
 H M/b + T2`4bi`B; B #B TQ (
 B 72Hb2 @ pt Hmy2xk8 Q` v I yXk8 (y)
 (@ R bB#UR3yTfV Ry UHQuV Ry @ bB#UR3yTfV Ry HMUVVV)
)
 H M/b + T2`4bi`B; B #B TQ (
 Ut k Y v kV Y UU yX8 tV Y Uy X8 k v VV k Y UU yX8 tV Y Uy X8
 v VV 9
)
 c Pi?2`rBb@b2` M/QK M/b + T2
 (` M/QK @ M Qy` 8y)
 V
)
 c a K Q Q I@M i M/QK M/b + T2`#2i i2`pBbm HBx iBQM2 `+ 277B+B2M+v
 B7H M/b + T2`4M/QK(
 b FKB M@M@TQ7+92bp Hm2) b FT i+?2BM@` /Bmb b p Hm2 p Hm2 @
 ` M/QK @ 7H y i)
 ` 2T2 i Ry (/B77mb2 p Hm2 R)
)
 c 6B M?2 i`m 2#2b iT i+?U; H Q# KB M B/K# b 2/Q M?2 + ?Q b 2HM M/b + T2
 UB72Hb2
 c 6m M+iB QM@k ; H Q# KB M B K
 H M/b + T2`#4tQM@T] E+b2i`m 2@#2bi@T i+? KB M@M?@Qp7 Hm2)
 c 6m M+iB QM@k ; H Q# KB M B K
 H M/b + T2`#4Qb@B M]@Q` v
 H M/b + T2`#4QH/2`@i]#Q`2
 H M/b + T2`#4bi`B; B #B TQ (b2i`m 2@#2bi@T i+? KB M@M?@Qp7 Hm2)
 c >BKK2H#H bn9 ; H Q# KB M B K# m i8 2K2` ; 2m2iQ /Bb+`2iBx iBQM2` b
 H M/b + T2`#4KK2H#H(b2i`m 2@#2bi@T i+? KB M@M?@Qp7 Hm2)
 c 6m M+iB QM@Rk ; H Q# KB M B K
 H M/b + T2`#4bQ TQ (b2i`m 2@#2bi@T i+? KB M@M?@Qp7 Rk)

c 6 m M + i B Q B M i 2 e k ; H Q # K B M B K
 H M/b+ T 2 p B M + 2 M (i b 2 i i` m 2 @ # 2 b i @ T i + ? K B M T @ M @ D Q p j h m 2))

c H H Q i ? 2 + Q b i 7 m M + i B Q M p b 2 b B M ; H 2 B Q # K B M B K
 (b 2 i i` m 2 @ # 2 b i @ T i + ? T i + ? K B M T @ M @ D Q p j h m 2))

V

cc a + H Z i + ? 2 b Q H Q B i ? B M B M M / K t p H m 2 h B K B i 7 b Q ` p B b m H B b i T B n Q ` M Q b 2 b
 H 2 i K B M @ p H K B M (p H m 2 i 2 Q 2
 H 2 i K t @ p H K t (p H m 2 i + Q 2 b
 b F T i + ? 2 b
UB 7 2 H b 2
 c S ` Q # H 2 # K 2 i 2 ` p B b m H B b h B M H; B M 2 + Q H Q b + H 2
 H M/b+ T 2 4 F H 2 v Q `
 H M/b+ T 2 # 4 Q ? + ? 2 b p M R J R Q `
 H M/b+ T 2 / 4 Q b b @ B M] @ Q ` v
 H M/b+ T 2 / 4 K p M Y E Q `
 H M/b+ T 2 / 4 Q T r f 2 Q `
 H M/b+ T 2 b 4 ? 7 7 2 M X j k Q `
 H M/b+ T 2 b 4 ? 7 7 2 M X j 9 Q `
 H M/b+ T 2 p B M + 2 M i
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H K t @ p H)

c S ` Q # H 2 # K 2 i 2 ` p B b m H B b h B M b; m ` 2 Q Q i 2 + Q H Q b + H 2
 H M/b+ T 2 2 4 b Q K Q `
 H M/b+ T 2 2 4 ; ? Q H J 2 Q `
 H M/b+ T 2 ? 4 Q H / 2 ` @ i] # Q f 2
 H M/b+ T 2 K 4 B + ? H 2 j B Q `
 H M/b+ T 2 K 4 B b ? M X j e Q `
 H M/b+ T 2 T 4 ` b Q T Q j h I Q Q b
 H M/b+ T 2 x 4 F ? ` Q p
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H K t @ p H)

c S ` Q # H 2 # K 2 i 2 ` p B b m H B b h B M H; Q ; ` B i ? K b B + H 2
 H M/b+ T 2 # 4 H 2 Q `
 H M/b+ T 2 / 4 t Q M @ T j E f 2
 H M/b+ T 2 ; 4 H / b i 2 B M @] T Q B + 2
 H M/b+ T 2 # 4 Q J ? Q `
 H M/b+ T 2 ; 4 Q b 2 M #] Q + F
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H H Q ; K t @ p H R X y R)

H M/b+ T 2 ; 4 b i ` B ; B M Q `
 H M/b+ T 2 ; 4 b i ` B ; B @ 7 7 b] 2 Q `
 H M/b+ T 2 ; 4 b i ` B ; B # M T Q M
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H H Q ; K t @ p H R X y 8)

H M/b+ T 2 ? 4 B K K 2 H # H Q ` m
 H M/b+ T 2 H 4 2 p j v Q `
 H M/b+ T 2 K 4 i v b Q `
 H M/b+ T 2 K 4 B b ? M X j Q `
 H M/b+ T 2 b 4 T ? 2 ` 2 @ Q T 7 Q ` 2 i
 H M/b+ T 2 i 4 ` 2 2 @ ? m K K 2 H
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H H Q ; K t @ p H R X R)

H M/b+ T 2 ? 4 Q b F E Q `
 H M/b+ T 2 K 4 B b ? M X j 8
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H H Q ; K t @ p H R y X R)

c 6 Q ` M v Q i ? 2 T ` Q # H 2 h 2 H Q ; ` B i ? K B 2 f m H b i + H 2
 (b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H m 2 K B M @ p H H Q ; K t @ p H R y X y R V
 R X y 8)

V

)

cc a 2 i b T Q i H B ; Q M Q ` Q 7 7
 B 7 b T Q i H B ; ? i ` 4 n 2 (r i + ? Q M 2 @ i Q m 2 @ # 2 b i @ T i + ?)
 2 M /

c a ? Q ` i 2 b 2 i m T ` Q + 2 / m 7 Q ` b Q K 2 2 T ` 2 b 2 M i i B p M / b + T 2 Q # H 2 K b

k k

```

i Q b 2 i m T @ b 2 ` + ? @ H M / b + T 2 b @ b ? Q ` i
c a 2 i m Tr Q ` H / M / T i + ? b B x 2
` 2 b B x 2 @ r Q ` H / @ 8 y y 8 y y @ 8 y y 8 y y
b 2 i @ T i + ? @ b B x 2 + 2 H H @ b B x 2
/B b T H v

c * ` 2 i 2 i ? 2 k. H M / b + T 2 + Q ` / B M Q i ? 2 + ? Q b 2 + M Q b i 7 m M + i B Q M # Q m M /
+ Q M b i ` B M i b
b 2 i t v @ # Q m B 7 H b 2 @ p H H M 2 b + T 2 24 ; ? Q H J 2 ( 8 R k ) ( e )
b F T i + ? 2 b
b 2 i t T t + Q ` U t v @ # Q m M K b t @ T t + Q ` 
b 2 i v T v + Q ` U t v @ # Q m M K b t @ T v + Q `

b 2 i p H m 2 B 2 H b 2 @ p H m 2
H M / b + T 2 b 4 T ? 2 ] 2 (
B 7 2 H b 2 @ p U H m 4 2 8 V Q ` U v 4 8 V
( R y y )
( t k Y v k )
)
H M / b + T 2 b 4 T ? 2 ` 2 @ Q J 7 ( b 2 i
U t @ j y y U t v @ # Q M M @ T t + Q ` k Y U v Y j y y U t v @ # Q m M / b f
K t @ T t + Q ` k
)
H M / b + T 2 ` 4 b i ` B ; B M c L Q i 2 ? i / 2 ; ` 2 2 b M Q i / B M b - 2 M 2 2 / 2 7 Q ` i ? 2 + Q b 7 m M + i B Q M
k y Y U U t k V @ + Q H U U R 3 y T V U k T V t V V Y U U v k V @ R y
+ Q b U U R 3 y T V U k T V v V V
)
H M / b + T 2 ` 4 Q b 2 M # ] Q (+ F
R y y U v @ U t k V V k Y U R @ t V k
)
H M / b + T 2 ? 4 B K K 2 H # H m
U U t k V Y v @ R R V k Y U t Y U v k V @ d V k
)
H M / b + T 2 24 ; ? Q H J 2 ( c L Q i 2 ? i / 2 ; ` 2 2 b M Q i / B M b - 2 M 2 2 / 2 7 Q ` i ? 2 b B M # m M + i B Q M
U U @ t V b B M U U R 3 y T V b [ ` i U # b U t @ U v Y 9 d V V V V V @ U b B M 9 d V
U U R 3 y T V b [ ` i U # b U U t f k V Y U v Y 9 d V V V V
)
(` M / Q K @ M Q y 18 y H ) h ? 2 H b i + b 2 B b ` M / Q K M / b + T 2
V
)

B 7 H M / b + T 2 ` 4 M / Q K(
c a K Q Q I Q m i ? 2 ` M / Q K M / b + T 2
b F K B M @ M @ T Q 7 + 9 2 b p H m 2 ) b F T i + ? 2 B M @ ` / B m b b 2 i p ( H m 2 p H m 2 @
` M / Q K @ 7 H y ) )
` 2 T 2 i R y ( / B 7 7 m b 2 p H m 2 R )
)

c 6 B M i ? 2 i ` m 2 # 2 b i H Q + i B Q M
B 7 2 H b 2 M / b + T 2 ? 4 B K K 2 H # H m
c ] ? B K K 2 H # H 2 t B # B B b ; H Q # K B M B K 8 2 K 2 ` ; 2 m 2 i Q / B b + ` 2 i B b i B Q M
2 `` Q ` b
b 2 i i ` m 2 @ # 2 b i @ T i + ? K B M @ M ? @ Q p 7 H m 2 )
)
c H H Q i ? 2 + Q b i 7 m M + i B Q M b 2 b B M ; H 2 Q # K B M B K
b 2 i i ` m 2 @ # 2 b i @ T i + ? T K + B M @ Q 2 i M D @ + Q 7 Z ( p H m 2 )
)

c a + H 2 T i + ? 2 b Q H Q B i ? B M H m B K B i b
H 2 i K B M @ p H K B M ( p H m 2 ) 2 Q 7
H 2 i K t @ p H K t ( p H m 2 ) i + Q 7 Z b
b F T i + ? 2 b 2 i T + Q H Q ` b + H 2 @ + Q H Q ` v 2 H H Q r p H n # 2 K K B @ P @ H I R X H G ; )

c a 2 i b T Q i H B ; B 7 b r B i + ? 2 Q M
B 7 b T Q i H B ; ? i ` 4 n 2 ( r i + ? Q M 2 @ i Q m 2 @ # 2 b i @ T i + ? )
2 M /
cccccc1 L . P 6 6 A G & c c c c c
```


* ? T i 2 ` 9

a Q 7 i r ` 2 H B + 2 M b 2

CIAO p 2 ` b B Q M R X k 8

* Q T v ` B ; ? i Ü k y k 9 a 2 ` ; B Q _ Q D b @ : H 2 M Q - G B M / b v • H p ` 2 x - J

h ? B b T ` Q ; ` K B b 7 ` 2 2 b Q 7 i r ` 2 , v Q m + M ` 2 / B b i ` B # m i 2 B i M
i ? 2 i 2 ` K b Q 7 i ? 2 : L I : 2 M 2 ` H S m # H B + G B + 2 M b 2 b T m # H B b ? 2 /
6 Q m M / i B Q M - 2 B i ? 2 ` p 2 ` b B Q M j Q 7 i ? 2 G B + 2 M b 2 - Q ` U i v Q m `

h ? B b T ` Q ; ` K B b / B b i ` B # m i 2 / B M i ? 2 ? Q T 2 i ? i B i r B H H # 2 m b
L u q _ _ L h u c r B i ? Q m i 2 p 2 M i ? 2 B K T H B 2 / r `` M i v Q 7 J 1 _ * > L h
Q ` 6 A h L 1 a a 6 P _ S _ h A * I G _ S I _ S P a 1 X a 2 2 i ? 2 : L I : 2 M 2 ` H S
G B + 2 M b 2 7 Q ` K Q ` 2 / 2 i B H b X

u Q m b ? Q m H / ? p 2 ` 2 + 2 B p 2 / + Q T v Q 7 i ? 2 : L I : 2 M 2 ` H S m # H B -
i ? B b T ` Q ; ` K X A 7 M Q i - v Q m + M / Q r M H Q / B i 7 ` Q K ,
? i i T b , f f r r r X ; M m X Q ` ; f H B + 2 M b 2 b f ; X H @ j X y X 2 M X ? i K H